HMFC: Hybrid MODLEm – Fuzzy Classifier for Liver Diseases Diagnose

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Abstract. Diagnose of Common diseases like liver is very complicated because its symptoms can be vague and easily confused with other health problems. In some cases, a person may have no symptoms at all but the liver may already have suffered significant damage. Many mathematical approach can deal with vagueness and uncertainty like fuzzy set theory (FS), although FS is good for classification but it requires more knowledge and experience in setting rules of inference based. In this paper an intelligent diagnosing model called hybrid modlem2-fuzzy classifier (HFMC) is proposed to enhance risk classification accuracy of liver diseases. Rough set approaches (RST) used to generate automated perfect rules to improve accuracy of classification of FS. The proposed model implemented in two phases, in first phase rules generated by laplace-Modem2 and use other RST algorithms (LEM2, Laplace-Modlem2) as comparison way. In second phase build fuzzy inference system based on the rules generated in first phase. The proposed model gives result of 99.14% classification accuracy of rule generation.

Keywords: Rough Set theory, Fuzzy Set Theory, Uncertainty, Rules Generation, liver diseases, classification accuracy.

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1. Introduction

Many countries start a lot of initiatives to develop their health care systems with investments in health information technology (IT). The goal of these initiatives is to use technology to improve the health care system by reducing costs, increasing patient safety and improving quality of care. Improving health care is a common goal for these countries [1, 3, 5]. One of important field in health and medical care field is diseases diagnose process. Health-care professionals use symptoms, tests and signs as references that used to determine the most likely diagnosis when illness is exist. Symptoms are also used to create a list of the possible differential diagnoses. These differential diagnosis is the basic point to safe patient's life by choosing initial treatments. Liver disease is common and dangerous disease in recent years because pollution of water, air and food. Most of patients with liver disease have multiple symptom's forms and values, but these symptoms not appear at earlier stage. It also may cause vague and uncertain symptoms, as loss of energy and weakness [3]. So our goal to provide early liver diseases diagnose system with high accuracy no way for errors because it doesn't depend on physician's expert or knowledge. There are many researcher proposed heart and liver disease diagnose model. A Fuzzy Expert System for heart disease diagnosis is designed with accuracy of 94% while rules not extracted automatically but it based on knowledge of physicians [7]. A Decision support system has been proposed for diagnosis of Congenital Heart Disease based on fuzzy set theory with 90% classification accuracy [18]. Computational intelligence techniques for Liver Patient Classification are presented which evaluates the selected classification algorithms (J-48, Multi-Layer Perceptron, Support Vector Machine, Random Forest and Bayesian Network) for the classification of liver patient datasets [6]. A fuzzy expert system for the diagnosis of Cirrhosis is designed. Numbers of rules used are 85 rules in this system and this large number which lake of accuracy and it lead to time consuming [9]. An intelligent diagnosis system for liver disease is proposed based on artificial neural network, rough and fuzzy set. But Using LEM algorithm lead to 6 rules are generated with accuracy of 96% and this not a correct classification [2].

A short summary on the use of rough sets in the medical informatics domain presented, focusing on applications of medical image segmentation, pattern classification and computer assisted medical decision making presented in [13]. The previous show importance of Knowledge discovery techniques in business and medical development in recent days. It is becoming very effective one in extract useful and meaningful information. There are many researchers are interested in proposing models based on discovery knowledge approaches. Pawlak present a lot of Rough sets benefits in [19]. RST algorithms are included in a lot of proposed hybrid techniques in knowledge discovery area. RST is an effective
technique when compared with other approaches [15]. RST discovered as very useful and effective technique for rule generations and attribute selection. Classification techniques and reduction algorithms presented with RST development in [19]. Intelligent models are proposed for diagnose diseases based on RST and its hybridization [21].

The aim of this study is to build a hybrid model–fuzzy classifier (HFMC) for liver diseases by combining RS approaches which known as Modified Lem2 (MODLEM2) under Laplace measure and fuzzy set. The model is proposed to analyzes the liver data and generate rules automatically and employ it in inference based of fuzzy set. This model can aid in prediction of the Pathological risk stages of the patient.

The rest of the paper is described as follows: In Section 2 the basic concept of rough set theory is presented; Section 3 presents LEM2 algorithm; section 4 presents Modified Lem2 (MODLEM2); section 5 presents fuzzy set theory concept. Section 6 presents the proposed model HFMC the liver diseases diagnoses section 7 presents the experimental results of proposed model. Finally Section 8 shows the conclusion of this paper

2. Rough Set Theory Concepts

Rough set is defined by topological operations called approximations that have pair of basic concepts, named the lower and the upper approximations of sets [8] as shown in figure 1.

RST depend on equivalence relation R or indiscernibility relation \( I_q \) to define the knowledge from data table which is 4-tuple information system IS = \((U, Q, V, f)\)

For each set of attributes \( Q \subset C \) an indiscernibility relation \( I_q \) is defined in the following way: two objects, \( x_i \) and \( x_j \) are indiscernible by the set of attributes \( Q \) in \( C \) if \( f(x_i, q) = f(x_j, q) \) for every \( q \subset C \). \( I_q \) has equivalence class which called elementary set or knowledge granules in \( q \) because it shows the smallest discernible groups of objects. For any element \( x_i \) of \( C \), the equivalence class of \( x_i \) in relation \( I_q \) is showed as \( [x_i]_{I_q} \). An indiscernibility relation formed as follows:

\[
I_q = \{ (x_i, x_j) \in U \times U : f(x_i, q) = f(x_j, q) \text{ for every } q \subset Q \} \tag{1}
\]

2.1. Lower and Upper Approximations

Lower approximation of \( \text{Cl} \) denoted by \( \overline{P} (\text{Cl}) \) and the P-upper approximation of \( \text{Cl} \) denoted by \( \overline{P} (\text{Cl}) \). As shown in figure 2 the Lower and upper approximation can be defined, respectively, as:

\[
\overline{P} (\text{Cl}) = \{ x \in U : I_q (x) \subseteq \text{Cl} \} \tag{2}
\]

\[
\overline{P} (\text{Cl}) = \{ x \in U : I_q (x) \cap \text{Cl} = \emptyset \} \tag{3}
\]

The elements of \( \overline{P} (\text{Cl}) \) are all and only objects \( x \in U \) which belong to the equivalence classes generated by the indiscernibility relation \( I_q \) contained in \( \text{Cl} \). The elements of \( \overline{P} (\text{Cl}) \) are all and only objects \( x \in U \) that belong to those equivalence classes generated by the indiscernibility relation \( I_p \) containing at least one object \( x \) belonging to \( \text{Cl} \).

The P-boundary of \( \text{Cl} \) denoted by \( B_{nP} (\text{Cl}) \), and is defined as:

\[
B_{nP} (\text{Cl}) = \overline{P} (\text{Cl}) - \overline{P} (\text{Cl}) \tag{4}
\]

Let us consider \( X \), subset of \( U \), \( X \subset U \).

The quality of approximation can be determined by lower and upper approximations [8,19]. The accuracy values range's is between (0, 1) and this show how the information derived from the original data.

\[
\text{The approximation accuracy} = \frac{\text{no of object that belongs to lower approximation}}{\text{no of object that belongs to upper approximation}} \tag{5}
\]

The quality of classification of decision class determined as:

\[
\text{The classification accuracy} = \frac{\text{no of object that correctly classified}}{\text{no of object in U}} \tag{6}
\]
The approximation accuracy determined based on attributes set whether the set is a rough (accuracy ≠1) or a crisp [20].

2.2. Core and Reduct of Attributes

There are a subset of attributes which fully describes the knowledge in the dataset; those attribute set is called a reduct [19]. Reduct is a subset of attributes RED ⊆ P. The core is the intersection of all reducts. Attributes from RED cannot be removed from the data sample without deteriorating the knowledge to be discovered.

2.3. Decision Rules generation by Rough Approximations

The rules are generated in form of “if... then...”, when the condition part defines values defined by one or more condition attributes (C-elementary sets) and the decision part defines an assignment to one or more decision classes (D-elementary sets).

The generated rules extracted by different RST algorithm have three types Minimum set of rules (LEM2 algorithm) [4], Exhaustive rules (modlem2 algorithm) and satisfactory rules (satisfactory algorithm) [19]. This discretization process is very important process to converting numerical attribute to nominal attribute [16]. Many of RST algorithms developed for generate decision rules

3. LEM2 Algorithm

LEM2 (Learning from Examples Module version-2) is used as modules in the algorithm LERS for learning from examples based on rough set. LEM2 computes a local covering followed by converting them to rule sets. The set of all cases labeled with the same decision value is called a concept. For attribute value pair (q, v), denoted [q], is the set of all examples that have attribute q have value v. Let B be a concept and let T be a set of attribute-value pairs. Concept B depends on a set T if and only if

$$\emptyset \neq [T] = \bigcap_{t \in T} [t] \subseteq B$$

(7)

Set T is said to be a minimal complex of B if and only if B depends on T and T is minimal. Let τ be a non-empty collection of non-empty sets of attribute value pairs. We say that τ is a local covering of B if and only if each member T of τ is a minimal complex of B, \(\bigcup_{T \in \tau} [T] = B\), and τ is minimal, i.e., τ has the smallest possible number of elements [10, 22].

For each concept B the LEM2 induced rules by computing local covering τ. Any set T, a minimal complex which is a member of τ is computed from attribute-value pairs selected from the set T(G) of attribute-value pairs relevant with a current goal G, i.e., pairs whose blocks have nonempty intersection with G. The initial goal G is equal to the concept and then it is iteratively updated by subtracting from G the set of examples described by the set of minimal complexes computed so far. Attribute-value pairs from T which are selected as the most relevant, i.e., on the basis of maximum of the cardinality of [q] \(\cap G\) if a tie occur, on the basis of the smallest cardinality of [q]. The last condition is equivalent to the maximal conditional probability of goal G , given attribute-value pair t.

LEM2 algorithms described as follow:

Procedure LEM2

Input: a set B;
Output: a single local covering T of set B;
Begin
G := B;
T := \emptyset;
While G ≠ \emptyset do
T := \emptyset;
G := B;
T := T \cup \{t\};
For each t in T do
if [T \{t\}] \subseteq then T := T \{t\};
end{while};
For each t in T do
if Us \{r\} \subseteq then T := T \r\{t\};
end{while};
end{procedure}

4. MODLEM2 Algorithm

MODLEM (Modified Learning from Examples Module) is an extension of Lem2 algorithm. MODLEM appeared despite it can generate rules from numerical and missing values of attribute but it requires preliminary preprocessing. In latest years MODLEM2(Modified Learning from Examples Module, version2) not require preliminary preprocessing because it was combined with local approximations that use attribute-value pairs which known as MODLEM-Entropy and MODLEM-Laplace. MODLEM2 can treat with attribute's continuous values without need of preliminary discretization and extract extended minimal rules. MODLEM2 is able to generate rule in form of at most and at least instead the simple form of equality like LEM2 as follow:

Attribute ≤ value; attribute ≥ value or lower bound ≤ attribute ≤ upper bound.
Entropy measure generate rules covering only small number of examples [10, 11]. Theses rule’s conditions constructed on cutting points that reduce the value of Entropy measure. The generated conditions have the syntax value ≤ attribute or attribute ≤ value.

Laplace measure which preferring higher values of Laplace accuracy to generate rules than entropy. In Laplace rule’s conditions constructed on cutting points that reduce the value of Laplace measure. The generated conditions have the syntax value ≤ attribute or attribute ≤ value.

MODLEM2- entropy measure is better in generating rule strength than Laplace measure while Laplace method is better than entropy method in inducing the number of rules [11, 12]. MODLEM2 algorithms described as follow:

Procedure MODLEM
Input: a set B; a set C of attributes
Output: a single local converting T of set B;
begin
G := B ;
T := ø;
While G ≠ ø do
    T := ø; {candidate of condition part of the rule}
    S:= U; { set of objects currently covered by T}
    While T = ø or not ([T] ⊆ B) do
        t := ø; {candidate for elementary condition}
        t_eval := ∞; { evaluation measure for t}
        for each attribute a ∈ C do
            Find_best_condition (a, S, new_t, t_eval_new_t); (look for best condition for a)
            If eval_new_t < t_eval then (evaluate if new condition is better than previous)
                t := new_t;
                t_eval := new_eval;
        end for;
        T := T ∪{t};
        S := S ∩{t};
    end{while not ([T] ⊆ B );
    For each elementary condition t ∈ T do
        If [T-{t}] ⊆ B then T := T-{t};
    T := T ∪[T]
    G := B - U_{t∈T} [T];
end{while C≠∅);
for each T ∈ D do
    if U_{t∈T}[t] = B then T:= T –{T};
end{ procedure}

Procedure Find_best_condition
input attribute a; set S of objects;
output current best condition best_t Evaluation measure eval_best_t of the best condition);
begin
    best_t := φ;
    eval_best_t := ∞;
    sort H; ( create a list of values for attribute a and objects from S sorted according to increasing values; H(i) is the ith value in the list)
    for i:= 1 to length (H) -1 do
        v := (H(i) +H(i+1))/2; {consider only mid-points between values characterizing examples belonging to different classes}
        S_1 := { x ∈ S | a(x) < v}; { |a(x) is the value of attribute a for object x}
        S_2 := { x ∈ S | a(x) ≥ v};
        eval_t := (|S_1|/| S_1∪ S_2|) *Ent(S_1) + (|S_2|/| S_1∪ S_2|) * Ent(S_2);
        (Ent entropy calculated for S_i)
        If eval_t < eval_best then
            If |C ∩ S_2| ≥ |C ∩ S_1| then
                Best_t := ( c ≥ v)
            else
                best_t := ( c < v);
        Eval_best_t := eval_t;
    end if
end

5. Fuzzy Set Theory Concept

The theory of fuzzy has advanced in different ways and in many applications [17]. It introduced by Zadehand Dieter Klaua that supports many concepts. Fs provide an important contribution in data mining to provide fuzzy data mining [14]. Fs are sets whose elements have membership degree. It is one on most important approach that can handle uncertainty, vagueness of any dataset. Fuzzy set theory supports concept of membership function for each element in set; the value of membership function interval [0, 1]. Fuzzy inference system is one of most approaches deal with uncertainty and vagueness which uses concept of FSs for diagrammatic representation and mapping from a given input to a driven output. FIS have two types of FIS Mamdani and Sugeno. Architecture of FIS is showed in figure 3. FS theory consists of:

- (Fuzzification process) input/output membership functions which refer to how to define the fuzzy set.
- Inference Base rules, in which generate rules Based on fuzzy logic/FSs operators.
- Defuzzification and output.
6. Hybrid Modlem2-Fuzzy Classifier for Liver Diseases Diagnoses Model (HMFC)

The aim of this study diagnose liver diseases based on hybrid Modlem2-Fuzzy classifier (HMFC) as shown in figure 4. This proposed model consist of two phases. First phase is rules generation using Laplace-Modlem2 algorithm then compare result with different RST approaches (LEM2 and Entropy-Modlem2). In the second phase FIS used as classifier to diagnose liver diseases.

6.1. A Case Study of Liver Diseases Diagnoses

The dataset was collected from medical data warehouse of liver disease. Dataset consist of 466 cases, it consists of five measured variables as follow:

- Total Bilirubin: in the total bilirubin there are three values refers to low, medium and high.
- Serum Albumin: the Serum albumin is one of most vital factor that effect on liver which has three values that refer to high, medium and low.
- Prothrombin Time (PT): is a blood test that measures the time it takes for the blood plasma to coagulate. It has three values which refer to high, medium and low.
- Ascites: It usually occurs when the liver stops working correctly; this lead to pain and swelling in the abdomen, And Queasiness. It has three values that refer to high, Medium and low.
- Hepatic Encephalopathy: it decrease function of brain that come as a result of highly liver disease, it has three values refer to high, medium and low.

Result is the decision attribute, it refer to levels of liver risk that has values (A, B, C) refer to low risk, moderate risk, high risk.

6.1.1. Data Preprocessing

Data are processed before used in our model based on The Child-Pugh score which consists of five clinical features that used to assess the prognosis of chronic liver disease and cirrhosis. Table.1 presents the Child-Pugh score for liver diseases.

<table>
<thead>
<tr>
<th>Factor</th>
<th>1 point</th>
<th>2 point</th>
<th>3 point</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total bilirubin (μmol/L)</td>
<td>&lt;34</td>
<td>34-50</td>
<td>&gt;50</td>
</tr>
<tr>
<td>Serum albumin (g/L)</td>
<td>&gt;35</td>
<td>28-35</td>
<td>&lt;28</td>
</tr>
<tr>
<td>PT INR</td>
<td>&lt;1.7</td>
<td>1.71-2.30</td>
<td>&gt;2.30</td>
</tr>
<tr>
<td>Ascites</td>
<td>None</td>
<td>Mild</td>
<td>Grade III-V (refractory)</td>
</tr>
<tr>
<td>Hepatic encephalopathy</td>
<td>None</td>
<td>Grade I-II (or suppressed with medication)</td>
<td>Grade III-V (or refractory)</td>
</tr>
</tbody>
</table>

The result is the output which has A, B, C classes based on Child-Pugh score, class A refers to total point (5-6), class B refers to total point (7-9) and finally class C refers to total point (10-15). Figure 5 shows liver diseases attributes with its nominal values after preprocessing and scoring step. decision attribute is result, risk values (A, B, C) refer to different liver diseases risk levels which mean low risk, moderate risk, high risk.
6.1.2. First Phase

In this phase we generate automated rules using different rough set algorithms. The rules generated by MODLEM2 algorithm with its two measures (Entropy & Laplace) then use LEM2 algorithm as a comparison method to ensure efficiency of generated rules. But to generate perfect minimal rules we must ensure accuracy of approximation.

Accuracy of Approximation. The quality of approximation for (A, B, C) decision classes is presented in Table 2 as below.

<table>
<thead>
<tr>
<th>class</th>
<th>No. object</th>
<th>Lower approximation</th>
<th>Upper approximation</th>
<th>accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>12</td>
<td>10</td>
<td>14</td>
<td>0.71</td>
</tr>
<tr>
<td>B</td>
<td>76</td>
<td>74</td>
<td>74</td>
<td>0.94</td>
</tr>
<tr>
<td>C</td>
<td>378</td>
<td>378</td>
<td>378</td>
<td>1</td>
</tr>
</tbody>
</table>

Total Quality Of Approximation : 99.1%

The approximation results indicate perfect accuracy for the three classes. Class "A" is the "low risk" class. There are 12 objects belonging to that class while upper approximation has 10 object and lower approximation include 14 object, so the approximation accuracy for "A" is 0.71. Class "B" means the "moderate risk" class, which accuracy reaches to 0.94. The accuracy of "C" class is one that refers to "high risk".

Rule Generation. We generates rules using MODLEM2. Based on laplace and entropy measures to extract the "extended minimum cover rules" then use LEM2 algorithm to generate minimal covering rules for comparing accuracy result.

6.1.2.1. Rules Generated by MODLEM2 Entropy measure.

The total number of rules generated by entropy measures is 23 rules. Sample of these rules are shown in Table 3.

<table>
<thead>
<tr>
<th>Id</th>
<th>Condition</th>
<th>Decision</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>(SerumAlbmin in {1,2}) &amp; (ProthrombinTime = 1) &amp; (HepaticEncehalopathy in {1,2}) &amp; (Ascites = 2) &amp; (HepaticEncehalopathy = 2)</td>
<td>Result= A</td>
</tr>
<tr>
<td>2</td>
<td>SerumAlbmin = 1 &amp; ProthrombinTime = 1 &amp; (HepaticEncehalopathy = 2)</td>
<td>Result= A</td>
</tr>
<tr>
<td>3</td>
<td>(TotalBiliurbin = 2) &amp; (SerumAlbmin = 1) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= A</td>
</tr>
<tr>
<td>4</td>
<td>TotalBiliurbin = 1 &amp; (SerumAlbmin = 2) &amp; (Ascites = 1) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= A</td>
</tr>
<tr>
<td>5</td>
<td>(TotalBiliurbin = 1) &amp; (SerumAlbmin = 1) &amp; (ProthrombinTime = 2) &amp; (Ascites = 1)</td>
<td>Result= A</td>
</tr>
<tr>
<td>6</td>
<td>(TotalBiliurbin = 1) &amp; (ProthrombinTime = 3) &amp; (Ascites = 1) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= B</td>
</tr>
<tr>
<td>7</td>
<td>(TotalBiliurbin = 1) &amp; (ProthrombinTime = 3) &amp; (HepaticEncehalopathy = 2)</td>
<td>Result= B</td>
</tr>
<tr>
<td>8</td>
<td>(TotalBiliurbin = 2) &amp; (SerumAlbmin = 3) &amp; (Ascites = 1)</td>
<td>Result= B</td>
</tr>
<tr>
<td>9</td>
<td>(TotalBiliurbin = 2) &amp; (SerumAlbmin in {2,3}) &amp; (Ascites in {1,2}) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= B</td>
</tr>
</tbody>
</table>

The accuracy of classification of entropy-modlem2 is validated with k-fold cross validation technique in 22 second with classification accuracy 98.27% as shown in figure 6.

Average Accuracy [k]

<table>
<thead>
<tr>
<th></th>
<th>Correct</th>
<th>Incorrect</th>
<th>None</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total</td>
<td>98.27%</td>
<td>1.73%</td>
<td>0.00%</td>
</tr>
<tr>
<td>A</td>
<td>63.33%</td>
<td>45.83%</td>
<td>0.00%</td>
</tr>
<tr>
<td>B</td>
<td>95.11%</td>
<td>4.99%</td>
<td>0.00%</td>
</tr>
<tr>
<td>C</td>
<td>100.00%</td>
<td>0.00%</td>
<td>0.00%</td>
</tr>
</tbody>
</table>

Time elapsed: 0.00:22 (22 seconds)

Figure 6. Entropy-DOMLEM classification accuracy.

6.1.2.2. Rules Generated by MODLEM2 Laplace measure.

The total number of rules generated by Laplace measures is 28 rules. Sample of these rules shown in Table 4.

<table>
<thead>
<tr>
<th>Id</th>
<th>Condition</th>
<th>Decision</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>(TotalBiliurbin = 2) &amp; (SerumAlbmin = 1) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= A</td>
</tr>
<tr>
<td>2</td>
<td>(TotalBiliurbin = 1) &amp; (SerumAlbmin = 2) &amp; (Ascites = 1) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= A</td>
</tr>
<tr>
<td>3</td>
<td>(TotalBiliurbin = 1) &amp; (ProthrombinTime = 1) &amp; (HepaticEncehalopathy = 2)</td>
<td>Result= A</td>
</tr>
<tr>
<td>4</td>
<td>(TotalBiliurbin = 1) &amp; (SerumAlbmin = 1) &amp; (ProthrombinTime = 1) &amp; (Ascites = 2)</td>
<td>Result= A</td>
</tr>
<tr>
<td>5</td>
<td>(TotalBiliurbin = 1) &amp; (SerumAlbmin = 1) &amp; (ProthrombinTime = 2) &amp; (Ascites = 1)</td>
<td>Result= B</td>
</tr>
<tr>
<td>6</td>
<td>(TotalBiliurbin = 1) &amp; (ProthrombinTime = 3) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= B</td>
</tr>
<tr>
<td>7</td>
<td>(TotalBiliurbin = 1) &amp; (ProthrombinTime = 3) &amp; (HepaticEncehalopathy = 2)</td>
<td>Result= B</td>
</tr>
<tr>
<td>8</td>
<td>(TotalBiliurbin = 2) &amp; (SerumAlbmin = 3) &amp; (Ascites = 1)</td>
<td>Result= B</td>
</tr>
<tr>
<td>9</td>
<td>(TotalBiliurbin = 2) &amp; (SerumAlbmin in {2,3}) &amp; (Ascites in {1,2}) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= B</td>
</tr>
</tbody>
</table>

The accuracy of classification of modlem2-laplace is validated with k-fold cross validation technique with 99.1% and elapsed time 21 second as shown in figure 7.

Average Accuracy [k]

<table>
<thead>
<tr>
<th></th>
<th>Correct</th>
<th>Incorrect</th>
<th>None</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total</td>
<td>99.14%</td>
<td>0.86%</td>
<td>0.00%</td>
</tr>
<tr>
<td>A</td>
<td>60.00%</td>
<td>40.00%</td>
<td>0.00%</td>
</tr>
<tr>
<td>B</td>
<td>96.32%</td>
<td>3.68%</td>
<td>0.00%</td>
</tr>
<tr>
<td>C</td>
<td>99.73%</td>
<td>0.27%</td>
<td>0.00%</td>
</tr>
</tbody>
</table>

Time elapsed: 0.00:21 (21 seconds)

Figure 7. Laplace - DOMLEM classification accuracy.
6.1.2.3. Rules Generated by LEM2

Rules generated with this algorithm are minimal rules. This means the set of rules does not have any redundant rules, and these rules are certain, such that there are a total of 31 rules generated from the data. The following table 5 shows sample of the minimum cover rules obtained (about 10 rules).

<table>
<thead>
<tr>
<th>Id</th>
<th>Condition</th>
<th>Decision</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>(TotalBiliurbin = 1) &amp; (ProthrombinTime = 1) &amp; (HepaticEncehalopathy = 2)</td>
<td>Result= A</td>
</tr>
<tr>
<td>2</td>
<td>(TotalBiliurbin = 1) &amp; (SerumAlbmin = 2) &amp; (ProthrombinTime = 1) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= A</td>
</tr>
<tr>
<td>3</td>
<td>(TotalBiliurbin = 1) &amp; (ProthrombinTime = 2) &amp; (Ascites = 1) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= A</td>
</tr>
<tr>
<td>4</td>
<td>(TotalBiliurbin = 1) &amp; (ProthrombinTime = 1) &amp; (Ascites = 2) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= B</td>
</tr>
<tr>
<td>5</td>
<td>(TotalBiliurbin = 2) &amp; (SerumAlbmin = 1) &amp; (Ascites = 1) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= A</td>
</tr>
<tr>
<td>6</td>
<td>(TotalBiliurbin = 2) &amp; (ProthrombinTime = 1) &amp; (Ascites = 1) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= A</td>
</tr>
<tr>
<td>7</td>
<td>(TotalBiliurbin = 3) &amp; (SerumAlbmin = 1) &amp; (Ascites = 1)</td>
<td>Result= B</td>
</tr>
<tr>
<td>8</td>
<td>(TotalBiliurbin = 1) &amp; (ProthrombinTime = 1) &amp; (Ascites = 3) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= B</td>
</tr>
<tr>
<td>9</td>
<td>(TotalBiliurbin = 1) &amp; (ProthrombinTime = 1) &amp; (Ascites = 1) &amp; (HepaticEncehalopathy = 3)</td>
<td>Result= B</td>
</tr>
<tr>
<td>10</td>
<td>(TotalBiliurbin = 2) &amp; (Ascites = 2) &amp; (HepaticEncehalopathy = 1)</td>
<td>Result= B</td>
</tr>
</tbody>
</table>

The classification accuracy of rules generated using LEM2 algorithm is 98.7%. Figure 8 show the result of k-fold cross validation technique for rules generated that validates result in 16 second.

<table>
<thead>
<tr>
<th>Average Accuracy [%]</th>
<th>Correct</th>
<th>Incorrect</th>
<th>None</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total</td>
<td>90.71%</td>
<td>1.72%</td>
<td>1.72%</td>
</tr>
<tr>
<td>A</td>
<td>60.00%</td>
<td>48.59%</td>
<td>10.05%</td>
</tr>
<tr>
<td>B</td>
<td>30.86%</td>
<td>3.94%</td>
<td>1.54%</td>
</tr>
<tr>
<td>C</td>
<td>39.46%</td>
<td>1.62%</td>
<td>0.54%</td>
</tr>
</tbody>
</table>

Time elapsed: 0:00:16 (15 seconds)

Figure 8. LEM2 result of cross-fold validation technique.

6.1.2.4. Comparison Between Proposed Algorithms

Finally as comparison between the three algorithms LEM2, MODLEM2 with ENTROPY and MODLEM2 with LAPLACE, we find that the second algorithm (MODLEM2) is the better algorithm in number of rule generated and accuracy of classification that needed for diagnose of liver diseases. we find that entropy–modlem2 is the best in number of rules while the laplace-modlem is the best in classification accuracy. so we will use laplace–modlem2 in our proposed HMFC based on its perfect accuracy.

6.1.3. Second Phase

In this phase we develop FIS for diagnose or classify pathological stages of liver diseases through using the rules generated in first phase from Laplace-modlem2 algorithm in FIS as inference rule based without need to external expert of physicians. We develop the fuzzy expert system by defining Membership functions, fuzzy rule base, fuzzification and defuzzification.

We firstly, construct the membership functions for five input variables and one output variable. Then rules generated from the first phase are employed as inference rule base. In the last step classification result are generated in form of defuzzification.

6.1.3.1. Input Variables

We will present five input variable with their fuzzy set ranges and their membership function for all of these sets in FIS. First input variable is Total Bilirubin which its Fuzzy set ranges are shown in Table 6. While the membership functions are trapezoidal and triangular for these fuzzy sets as shown in figure 9.

<table>
<thead>
<tr>
<th>Table 6. Total bilirubin’s Fuzzy sets.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Input variable</td>
</tr>
<tr>
<td>----------------</td>
</tr>
<tr>
<td>Total Bilirubin</td>
</tr>
<tr>
<td></td>
</tr>
<tr>
<td></td>
</tr>
</tbody>
</table>

Figure 9. Membership function of Total Bilirubin.

Second input variable is Serum Albumin which its Fuzzy set ranges are shown in table 7. While the membership functions are trapezoidal and triangular as shown in figure 10.

<table>
<thead>
<tr>
<th>Table 7. Serum Albumin Fuzzy sets.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Input variable</td>
</tr>
<tr>
<td>----------------</td>
</tr>
<tr>
<td>Serum Albumin</td>
</tr>
<tr>
<td></td>
</tr>
<tr>
<td></td>
</tr>
</tbody>
</table>

Figure 10. Membership function of Serum Albumin.

The classification accuracy of rules generated using MODLEM2 algorithm is 98.7%. Figure 8 show the result of k-fold cross validation technique for rules generated that validates result in 16 second.
Third input variable is Prothrombin Time which its Fuzzy set ranges are shown in table 8. Membership functions are trapezoidal and triangular for fuzzy sets as shown in figure 11.

Table 8. Prothrombin Time Fuzzy sets.

<table>
<thead>
<tr>
<th>Input variable</th>
<th>range</th>
<th>Fuzzy set</th>
</tr>
</thead>
<tbody>
<tr>
<td>Prothrombin Time</td>
<td>&gt;$4.0$</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>4.0-6.0</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>&gt;$6$</td>
<td>3</td>
</tr>
</tbody>
</table>

Figure 11. Membership function of Prothrombin Time.

Fourth input variable is Ascites which its Fuzzy set ranges are shown in table 9 while Membership functions for fuzzy sets are trapezoidal and triangular as shown in figure 12.

Table 9. Ascites Fuzzy sets.

<table>
<thead>
<tr>
<th>Input variable</th>
<th>range</th>
<th>Fuzzy set</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ascites</td>
<td>none ($&lt;2$)</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>mild (2.0-3.0)</td>
<td>2</td>
</tr>
</tbody>
</table>

Figure 12. Membership function of Ascites.

Fifth input variable is Hepatic Encephalopathy which its Fuzzy set ranges are shown in table 10. Membership functions are trapezoidal and triangular for fuzzy sets as shown in figure 13.

Table 10. Hepatic Encephalopathy Fuzzy sets.

<table>
<thead>
<tr>
<th>Input variable</th>
<th>range</th>
<th>Fuzzy set</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hepatic Encephalopathy</td>
<td>None</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>Grade I-II (2-3)</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>Grade III IV (&gt;3)</td>
<td>3</td>
</tr>
</tbody>
</table>

Figure 13. Membership function of Hepatic Encephalopathy.

6.1.3.3. Fuzzy Rule Base

The rules which generated before through first phase with RST using laplace-modlem2 algorithm are entered to FIS system as fuzzy rule base. The rule base consists of 28 well defined extended minimal rules that determine the risk stages. Sample of these rules in FIS is shown in Figure 15.

Figure 14. Membership function of Result.

6.1.3.4. Fuzzification and Defuzzification

Inference mechanism of our system relies on MAMDANI model. The FIS result of rules and surface viewer is shown in figure 16,17 and 18. Figure 16 represents that the liver risk with its values while total bilirubin is 40, Serum Albumin is 3.5, Prothrombin Time is 7.95, ascites is 2.57 and Hepatic Encephalopathy is 2.51 as tested data the result will be 12.3. Figure 17 and 18 represent the relation between different input variable and result output and how these symptoms effect on result of liver risks.

6.1.3.2. Output Variable

Our model proposed to identify pathologies risk stages of liver. The fuzzy set ranges of output in range [0, 15] as shown in table 11 while the Membership functions of these fuzzy sets are triangular and are shown in figure 14. Output's Fuzzy set A, B, C refers to Low risk, moderate risk and High risk.
7. Conclusion

This study builds robust expert system for diagnoses diseases of liver based on hybrid model Modlem2-fuzzy set HRFC. Since using RST or FS alone cannot provide accurate result and require more knowledge and experience. The proposed model improves fuzzy set while determining the content of the rules is usually achieved by knowledge acquisition with an expert which, for a large Application can be very time consuming, as well as not automated. HMFC has two stages, in first stage the laplace-modlem2 used mainly to automatic generation of extended minimal cover rules. In the second stage, construct fuzzy inference system for liver diseases through using rules generated by RST in first stage for diagnose or classify Pathological stages (risks) of the patient in liver diseases diagnose system. The experimental results presented in this study shows that the proposed HMFC model is better accuracy than using rough sets or fuzzy systems separately. When rules that differentiate between pathology stages of liver diseases are generated with 99.14% as classification accuracy this mean that combining rough set and fuzzy system approaches enhance classification accuracy.

References


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